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# Frequency of Under Damped Forced Vibrations Formulas

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## List of 15 Frequency of Under Damped Forced Vibrations Formulas

### Frequency of Under Damped Forced Vibrations

#### 1) Complementary Function

$$fx \quad x_1 = A \cdot \cos(\omega_d - \phi)$$

[Open Calculator !\[\]\(a870788d6ed9b8fd294b7654a8c8526b\_img.jpg\)](#)

$$ex \quad 2.527173m = 5.25m \cdot \cos(6Hz - 45^\circ)$$

#### 2) Damping Coefficient

$$fx \quad c = \frac{\tan(\phi) \cdot (k - m \cdot \omega^2)}{\omega}$$

[Open Calculator !\[\]\(c50c8b7b2cc2cf9ff925edec0ee94c0d\_img.jpg\)](#)

$$ex \quad 3.5Ns/m = \frac{\tan(45^\circ) \cdot (60N/m - .25kg \cdot (10rad/s)^2)}{10rad/s}$$

#### 3) Deflection of System under Static Force

$$fx \quad x_o = \frac{F_x}{k}$$

[Open Calculator !\[\]\(f60b7a900783ac3fd531bfd9c111be6d\_img.jpg\)](#)

$$ex \quad 0.333333m = \frac{20N}{60N/m}$$


#### 4) External Periodic Disturbing Force

$$fx \quad F = F_x \cdot \cos(\omega \cdot t_p)$$

[Open Calculator !\[\]\(83bbbd261710c59db0214aa27b2edc0d\_img.jpg\)](#)


$$ex \quad 16.87708N = 20N \cdot \cos(10rad/s \cdot 1.2s)$$



5) Maximum Displacement of Forced Vibration [Open Calculator !\[\]\(4729e517bc6a7cd81c8025b9646574fb\_img.jpg\)](#)

$$fx \quad d_{\text{mass}} = \frac{F_x}{\sqrt{(c \cdot \omega)^2 - (k - m \cdot \omega^2)^2}}$$

$$ex \quad 0.560112\text{m} = \frac{20\text{N}}{\sqrt{(5\text{Ns/m} \cdot 10\text{rad/s})^2 - (60\text{N/m} - .25\text{kg} \cdot (10\text{rad/s})^2)^2}}$$

6) Maximum Displacement of Forced Vibration at Resonance [Open Calculator !\[\]\(e474458956c9a37fbf9586ddb60a7fa1\_img.jpg\)](#)

$$fx \quad d_{\text{mass}} = x_o \cdot \frac{k}{c \cdot \omega_n}$$

$$ex \quad 0.188571\text{m} = 0.33\text{m} \cdot \frac{60\text{N/m}}{5\text{Ns/m} \cdot 21\text{rad/s}}$$

7) Maximum Displacement of Forced Vibration using Natural Frequency [Open Calculator !\[\]\(4fe57c3593bf1b21d272ae7ac8dfaf77\_img.jpg\)](#)

$$fx \quad d_{\text{mass}} = \frac{F_x}{\sqrt{(c \cdot \frac{\omega}{k})^2 + \left(1 - \left(\frac{\omega}{\omega_n}\right)^2\right)^2}}$$


$$ex \quad 17.59301\text{m} = \frac{20\text{N}}{\sqrt{(5\text{Ns/m} \cdot \frac{10\text{rad/s}}{60\text{N/m}})^2 + \left(1 - \left(\frac{10\text{rad/s}}{21\text{rad/s}}\right)^2\right)^2}}$$

8) Maximum Displacement of Forced Vibration with Negligible Damping [Open Calculator !\[\]\(2bae76de5ebbd5c4d7d47162f1673734\_img.jpg\)](#)

$$fx \quad d_{\text{mass}} = \frac{F_x}{m \cdot (\omega_n^2 - \omega^2)}$$

$$ex \quad 0.234604\text{m} = \frac{20\text{N}}{.25\text{kg} \cdot ((21\text{rad/s})^2 - (10\text{rad/s})^2)}$$



9) Particular Integral 

$$fx \quad x_2 = \frac{F_x \cdot \cos(\omega \cdot t_p - \phi)}{\sqrt{(c \cdot \omega)^2 - (k - m \cdot \omega^2)^2}}$$

Open Calculator 

$$ex \quad 0.121701m = \frac{20N \cdot \cos(10rad/s \cdot 1.2s - 45^\circ)}{\sqrt{(5Ns/m \cdot 10rad/s)^2 - (60N/m - .25kg \cdot (10rad/s)^2)^2}}$$

10) Phase Constant 

$$fx \quad \phi = a \tan\left(\frac{c \cdot \omega}{k - m \cdot \omega^2}\right)$$

Open Calculator 


$$ex \quad 55.00798^\circ = a \tan\left(\frac{5Ns/m \cdot 10rad/s}{60N/m - .25kg \cdot (10rad/s)^2}\right)$$

11) Static Force 

$$fx \quad F_x = x_o \cdot k$$

Open Calculator 

$$ex \quad 19.8N = 0.33m \cdot 60N/m$$

12) Static Force using Maximum Displacement or Amplitude of Forced Vibration 

$$fx \quad F_x = d_{mass} \cdot \left(\sqrt{(c \cdot \omega)^2 - (k - m \cdot \omega^2)^2}\right)$$

Open Calculator 

$$ex \quad 28.56571N = 0.8m \cdot \left(\sqrt{(5Ns/m \cdot 10rad/s)^2 - (60N/m - .25kg \cdot (10rad/s)^2)^2}\right)$$

13) Static Force when Damping is Negligible 

$$fx \quad F_x = d_{mass} \cdot (m \cdot \omega_n^2 - \omega^2)$$

Open Calculator 

$$ex \quad 8.2N = 0.8m \cdot (.25kg \cdot (21rad/s)^2 - (10rad/s)^2)$$



14) Total Displacement of Forced Vibration given Particular Integral and Complementary Function 

$$\text{fx } d_{\text{mass}} = x_2 + x_1$$

[Open Calculator !\[\]\(e2376d476d06eb31946dc01a69a4403a\_img.jpg\)](#)

$$\text{ex } 14.9\text{m} = 12.4\text{m} + 2.5\text{m}$$

15) Total Displacement of Forced Vibrations 

$$\text{fx } d_{\text{mass}} = A \cdot \cos(\omega_d - \phi) + \frac{F_x \cdot \cos(\omega \cdot t_p - \phi)}{\sqrt{(c \cdot \omega)^2 - (k - m \cdot \omega^2)^2}}$$

[Open Calculator !\[\]\(0b5e7e25e8775f7e7e80906ada4f0021\_img.jpg\)](#)

$$\text{ex } 2.648875\text{m} = 5.25\text{m} \cdot \cos(6\text{Hz} - 45^\circ) + \frac{20\text{N} \cdot \cos(10\text{rad/s} \cdot 1.2\text{s} - 45^\circ)}{\sqrt{(5\text{Ns/m} \cdot 10\text{rad/s})^2 - (60\text{N/m} - .25\text{kg} \cdot (10\text{rad/s})^2)^2}}$$












## Variables Used

- **A** Amplitude of Vibration (Meter)
- **c** Damping Coefficient (Newton Second per Meter)
- **d<sub>mass</sub>** Total Displacement (Meter)
- **F** External Periodic Disturbing Force (Newton)
- **F<sub>x</sub>** Static Force (Newton)
- **k** Stiffness of Spring (Newton per Meter)
- **m** Mass suspended from Spring (Kilogram)
- **t<sub>p</sub>** Time Period (Second)
- **x<sub>1</sub>** Complementary Function (Meter)
- **x<sub>2</sub>** Particular Integral (Meter)
- **x<sub>o</sub>** Deflection under Static Force (Meter)
- **ϕ** Phase Constant (Degree)
- **ω** Angular Velocity (Radian per Second)
- **ω<sub>d</sub>** Circular Damped Frequency (Hertz)
- **ω<sub>n</sub>** Natural Circular Frequency (Radian per Second)



## Constants, Functions, Measurements used

- **Function: atan**, atan(Number)  
*Inverse trigonometric tangent function*
- **Function: cos**, cos(Angle)  
*Trigonometric cosine function*
- **Function: sqrt**, sqrt(Number)  
*Square root function*
- **Function: tan**, tan(Angle)  
*Trigonometric tangent function*
- **Measurement: Length** in Meter (m)  
*Length Unit Conversion* 
- **Measurement: Weight** in Kilogram (kg)  
*Weight Unit Conversion* 
- **Measurement: Time** in Second (s)  
*Time Unit Conversion* 
- **Measurement: Force** in Newton (N)  
*Force Unit Conversion* 
- **Measurement: Angle** in Degree (°)  
*Angle Unit Conversion* 
- **Measurement: Frequency** in Hertz (Hz)  
*Frequency Unit Conversion* 
- **Measurement: Surface Tension** in Newton per Meter (N/m)  
*Surface Tension Unit Conversion* 
- **Measurement: Angular Velocity** in Radian per Second (rad/s)  
*Angular Velocity Unit Conversion* 
- **Measurement: Damping Coefficient** in Newton Second per Meter (Ns/m)  
*Damping Coefficient Unit Conversion* 



## Check other formula lists

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