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Structural Analysis of Beams Formulas

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List of 26 Structural Analysis of Beams Formulas

Structural Analysis of Beams

1) Area to Maintain Stress as Wholly Compressive given Eccentricity

$$fx \quad A = \frac{Z}{e'}$$

[Open Calculator !\[\]\(a870788d6ed9b8fd294b7654a8c8526b_img.jpg\)](#)

$$ex \quad 5600\text{mm}^2 = \frac{1120000\text{mm}^3}{200\text{mm}}$$

2) Beam Breadth of Uniform Strength for Simply Supported Beam when Load is at Centre

$$fx \quad B = \frac{3 \cdot P \cdot a}{\sigma \cdot d_e^2}$$

[Open Calculator !\[\]\(c50c8b7b2cc2cf9ff925edec0ee94c0d_img.jpg\)](#)

$$ex \quad 96.95291\text{mm} = \frac{3 \cdot 0.15\text{kN} \cdot 21\text{mm}}{1200\text{Pa} \cdot (285\text{mm})^2}$$

3) Beam Depth of Uniform Strength for Simply Supported Beam when Load is at Centre

$$fx \quad d_e = \sqrt{\frac{3 \cdot P \cdot a}{B \cdot \sigma}}$$

[Open Calculator !\[\]\(f60b7a900783ac3fd531bfd9c111be6d_img.jpg\)](#)

$$ex \quad 280.6239\text{mm} = \sqrt{\frac{3 \cdot 0.15\text{kN} \cdot 21\text{mm}}{100.0003\text{mm} \cdot 1200\text{Pa}}}$$

4) Breadth for Rectangular Section to Maintain Stress as Wholly Compressive

$$fx \quad t = 6 \cdot e'$$

[Open Calculator !\[\]\(83bbbd261710c59db0214aa27b2edc0d_img.jpg\)](#)

$$ex \quad 1200\text{mm} = 6 \cdot 200\text{mm}$$


5) Eccentricity for Rectangular Section to maintain Stress as Wholly Compressive

$$fx \quad e' = \frac{t}{6}$$

[Open Calculator !\[\]\(f507db636256ac11a5525ef93ec6b8d7_img.jpg\)](#)

$$ex \quad 200\text{mm} = \frac{1200\text{mm}}{6}$$




6) Eccentricity for Solid Circular Sector to Maintain Stress as Wholly Compressive 

$$fx \quad e' = \frac{\Phi}{8}$$

[Open Calculator !\[\]\(cbe80b694ebd74fcfe136a095b608235_img.jpg\)](#)

$$ex \quad 95\text{mm} = \frac{760\text{mm}}{8}$$

7) Eccentricity in Column for Hollow Circular Section when Stress at Extreme Fibre is Zero 

$$fx \quad e' = \frac{D^2 + d_i^2}{8 \cdot D}$$

[Open Calculator !\[\]\(3e2231b1ad3ca8da8658228c00dd08e0_img.jpg\)](#)

$$ex \quad 1281.25\text{mm} = \frac{(4000\text{mm})^2 + (5000\text{mm})^2}{8 \cdot 4000\text{mm}}$$

8) Eccentricity to Maintain Stress as Wholly Compressive 

$$fx \quad e' = \frac{Z}{A}$$

[Open Calculator !\[\]\(0d5ec72f61334709c3fc9450209b754f_img.jpg\)](#)


$$ex \quad 200\text{mm} = \frac{1120000\text{mm}^3}{5600\text{mm}^2}$$

9) Loading of Beam of Uniform Strength 

$$fx \quad P = \frac{\sigma \cdot B \cdot d_e^2}{3 \cdot a}$$

[Open Calculator !\[\]\(b64b40baaee5acddc1eab8538ba84754_img.jpg\)](#)

$$ex \quad 0.154715\text{kN} = \frac{1200\text{Pa} \cdot 100.0003\text{mm} \cdot (285\text{mm})^2}{3 \cdot 21\text{mm}}$$

10) Section Modulus to Maintain Stress as Wholly Compressive given Eccentricity 

$$fx \quad Z = e' \cdot A$$

[Open Calculator !\[\]\(aff7c69c44a5e015f18c35867ef3f5c3_img.jpg\)](#)

$$ex \quad 1.1\text{E}^6\text{mm}^3 = 200\text{mm} \cdot 5600\text{mm}^2$$

11) Stress of Beam of Uniform Strength 

$$fx \quad \sigma = \frac{3 \cdot P \cdot a}{B \cdot d_e^2}$$

[Open Calculator !\[\]\(a25a22d88c5882f4a20f36103df86562_img.jpg\)](#)

$$ex \quad 1163.431\text{Pa} = \frac{3 \cdot 0.15\text{kN} \cdot 21\text{mm}}{100.0003\text{mm} \cdot (285\text{mm})^2}$$



Continuous Beams

12) Absolute Value of Maximum Moment in Unbraced Beam Segment

$$\text{fx } M'_{\max} = \frac{M_{\text{coeff}} \cdot ((3 \cdot M_A) + (4 \cdot M_B) + (3 \cdot M_C))}{12.5 - (M_{\text{coeff}} \cdot 2.5)}$$

[Open Calculator !\[\]\(23d9fc146e83b5c3013cfa32c784f8d5_img.jpg\)](#)

$$\text{ex } 50.23317\text{N}^*\text{m} = \frac{1.32\text{N}^*\text{m} \cdot ((3 \cdot 30\text{N}^*\text{m}) + (4 \cdot 50.02\text{N}^*\text{m}) + (3 \cdot 20.01\text{N}^*\text{m}))}{12.5 - (1.32\text{N}^*\text{m} \cdot 2.5)}$$

13) Condition for Maximum Moment in Interior Spans of Beams

$$\text{fx } x'' = \left(\frac{\text{Len}}{2} \right) - \left(\frac{M_{\max}}{q \cdot \text{Len}} \right)$$

[Open Calculator !\[\]\(aa53ad6fea213b8b2226d3077e30533a_img.jpg\)](#)

$$\text{ex } 1.499666\text{m} = \left(\frac{3\text{m}}{2} \right) - \left(\frac{10.03\text{N}^*\text{m}}{10.0006\text{kN}/\text{m} \cdot 3\text{m}} \right)$$

14) Condition for Maximum Moment in Interior Spans of Beams with Plastic Hinge

$$\text{fx } x = \left(\frac{\text{Len}}{2} \right) - \left(\frac{k \cdot M_p}{q \cdot \text{Len}} \right)$$

[Open Calculator !\[\]\(626ce8ac21792b9405bfddfea8e0c96a_img.jpg\)](#)

$$\text{ex } 1.24984\text{m} = \left(\frac{3\text{m}}{2} \right) - \left(\frac{0.75 \cdot 10.007\text{kN}^*\text{m}}{10.0006\text{kN}/\text{m} \cdot 3\text{m}} \right)$$

15) Ultimate Load for Continuous Beam

$$\text{fx } U = \frac{4 \cdot M_p \cdot (1 + k)}{\text{Len}}$$

[Open Calculator !\[\]\(c1168d6a8b365d11e842ece304635fa7_img.jpg\)](#)

$$\text{ex } 23.34967\text{kN} = \frac{4 \cdot 10.007\text{kN}^*\text{m} \cdot (1 + 0.75)}{3\text{m}}$$

Elastic Lateral Buckling of Beams

16) Absolute Value of Moment at Centerline of Unbraced Beam Segment

$$\text{fx } M_B = \frac{(12.5 \cdot M'_{\max}) - (2.5 \cdot M'_{\max} + 3 \cdot M_A + 3 \cdot M_C)}{4}$$

[Open Calculator !\[\]\(c724c83fe216b2427610afdbd31f92cc_img.jpg\)](#)

$$\text{ex } 87.5175\text{N}^*\text{m} = \frac{(12.5 \cdot 50.01\text{N}^*\text{m}) - (2.5 \cdot 50.01\text{N}^*\text{m} + 3 \cdot 30\text{N}^*\text{m} + 3 \cdot 20.01\text{N}^*\text{m})}{4}$$




17) Absolute Value of Moment at Quarter Point of Unbraced Beam Segment 

$$\text{fx } M_A = \frac{(12.5 \cdot M'_{\max}) - (2.5 \cdot M'_{\max} + 4 \cdot M_B + 3 \cdot M_C)}{3}$$

Open Calculator 


$$\text{ex } 79.99667\text{N}^*\text{m} = \frac{(12.5 \cdot 50.01\text{N}^*\text{m}) - (2.5 \cdot 50.01\text{N}^*\text{m} + 4 \cdot 50.02\text{N}^*\text{m} + 3 \cdot 20.01\text{N}^*\text{m})}{3}$$

18) Absolute Value of Moment at Three-Quarter Point of Unbraced Beam Segment 

$$\text{fx } M_C = \frac{(12.5 \cdot M'_{\max}) - (2.5 \cdot M'_{\max} + 4 \cdot M_B + 3 \cdot M_A)}{3}$$

Open Calculator 


$$\text{ex } 70.00667\text{N}^*\text{m} = \frac{(12.5 \cdot 50.01\text{N}^*\text{m}) - (2.5 \cdot 50.01\text{N}^*\text{m} + 4 \cdot 50.02\text{N}^*\text{m} + 3 \cdot 30\text{N}^*\text{m})}{3}$$

19) Critical Bending Coefficient 

$$\text{fx } M_{\text{coeff}} = \frac{12.5 \cdot M'_{\max}}{(2.5 \cdot M'_{\max}) + (3 \cdot M_A) + (4 \cdot M_B) + (3 \cdot M_C)}$$

Open Calculator 

$$\text{ex } 1.315679\text{N}^*\text{m} = \frac{12.5 \cdot 50.01\text{N}^*\text{m}}{(2.5 \cdot 50.01\text{N}^*\text{m}) + (3 \cdot 30\text{N}^*\text{m}) + (4 \cdot 50.02\text{N}^*\text{m}) + (3 \cdot 20.01\text{N}^*\text{m})}$$

20) Critical Bending Moment for Simply Supported Open Section Beam 

$$\text{fx } M_{\text{cr}} = \left(\frac{\pi}{L}\right) \cdot \sqrt{E \cdot I_y \cdot \left((G \cdot J) + E \cdot C_w \cdot \left(\frac{\pi^2}{(L)^2}\right) \right)}$$

Open Calculator 

$$\text{ex } 9.802145\text{N}^*\text{m} = \left(\frac{\pi}{10.04\text{cm}}\right) \cdot \sqrt{10.01\text{MPa} \cdot 10.001\text{kg} \cdot \text{m}^2 \cdot \left((100.002\text{N}/\text{m}^2 \cdot 10.0001) + 10.01\text{MPa} \cdot 10.0005 \right)}$$


21) Critical Bending Moment for Simply Supported Rectangular Beam 

$$\text{fx } M_{\text{Cr(Rect)}} = \left(\frac{\pi}{L_{\text{en}}}\right) \cdot \left(\sqrt{e \cdot I_y \cdot G \cdot J}\right)$$

Open Calculator 

$$\text{ex } 740.5286\text{N}^*\text{m} = \left(\frac{\pi}{3\text{m}}\right) \cdot \left(\sqrt{50\text{Pa} \cdot 10.001\text{kg} \cdot \text{m}^2 \cdot 100.002\text{N}/\text{m}^2 \cdot 10.0001}\right)$$




22) Critical Bending Moment in Non-Uniform Bending 

$$\text{fx } M'_{cr} = (M_{\text{coeff}} \cdot M_{cr})$$

[Open Calculator !\[\]\(d3fb9f94af8b26d1c844efa9a98805b0_img.jpg\)](#)

$$\text{ex } 13.2N^*m = (1.32N^*m \cdot 10N^*m)$$

23) Elasticity Modulus given Critical Bending Moment of Rectangular Beam 

$$\text{fx } e = \frac{(M_{Cr(\text{Rect})} \cdot \text{Len})^2}{(\pi^2) \cdot I_y \cdot G \cdot J}$$

[Open Calculator !\[\]\(e1d6102fe77919492c04879c8450f1f5_img.jpg\)](#)


$$\text{ex } 50.06367Pa = \frac{(741N^*m \cdot 3m)^2}{(\pi^2) \cdot 10.001kg \cdot m^2 \cdot 100.002N/m^2 \cdot 10.0001}$$

24) Minor Axis Moment of Inertia for Critical Bending Moment of Rectangular Beam 

$$\text{fx } I_y = \frac{(M_{Cr(\text{Rect})} \cdot \text{Len})^2}{(\pi^2) \cdot e \cdot G \cdot J}$$

[Open Calculator !\[\]\(ab4e2b3fc7e7887b7a72f548aa6f5e60_img.jpg\)](#)


$$\text{ex } 10.01374kg \cdot m^2 = \frac{(741N^*m \cdot 3m)^2}{(\pi^2) \cdot 50Pa \cdot 100.002N/m^2 \cdot 10.0001}$$

25) Shear Elasticity Modulus for Critical Bending Moment of Rectangular Beam 

$$\text{fx } G = \frac{(M_{Cr(\text{Rect})} \cdot \text{Len})^2}{(\pi^2) \cdot I_y \cdot e \cdot J}$$

[Open Calculator !\[\]\(5abce1a84a655b073239ab33e1199487_img.jpg\)](#)

$$\text{ex } 100.1294N/m^2 = \frac{(741N^*m \cdot 3m)^2}{(\pi^2) \cdot 10.001kg \cdot m^2 \cdot 50Pa \cdot 10.0001}$$

26) Unbraced Member Length given Critical Bending Moment of Rectangular Beam 

$$\text{fx } \text{Len} = \left(\frac{\pi}{M_{Cr(\text{Rect})}} \right) \cdot \left(\sqrt{e \cdot I_y \cdot G \cdot J} \right)$$

[Open Calculator !\[\]\(111c5272ee3f91361f0d2e3665dd6ad0_img.jpg\)](#)

$$\text{ex } 2.998092m = \left(\frac{\pi}{741N^*m} \right) \cdot \left(\sqrt{50Pa \cdot 10.001kg \cdot m^2 \cdot 100.002N/m^2 \cdot 10.0001} \right)$$











Variables Used

- **a** Distance from A end (Millimeter)
- **A** Area of Cross-Section (Square Millimeter)
- **B** Width of Beam Section (Millimeter)
- **C_w** Warping Constant (Kilogram Square Meter)
- **D** Outer Depth (Millimeter)
- **d_e** Effective Depth of Beam (Millimeter)
- **d_i** Inner Depth (Millimeter)
- **e** Elastic Modulus (Pascal)
- **e'** Eccentricity of Load (Millimeter)
- **E** Modulus of Elasticity (Megapascal)
- **G** Shear Modulus of Elasticity (Newton per Square Meter)
- **I_y** Moment of Inertia about Minor Axis (Kilogram Square Meter)
- **J** Torsional Constant
- **k** Ratio between Plastic Moments
- **L** Unbraced Length of Member (Centimeter)
- **Len** Length of Rectangular Beam (Meter)
- **M_A** Moment at Quarter Point (Newton Meter)
- **M_B** Moment at Centerline (Newton Meter)
- **M_C** Moment at Three-quarter Point (Newton Meter)
- **M_{coeff}** Bending Moment Coefficient (Newton Meter)
- **M_{cr}** Critical Bending Moment (Newton Meter)
- **M'_{cr}** Non-Uniform Critical Bending Moment (Newton Meter)
- **M_{Cr(Rec)}** Critical Bending Moment for Rectangular (Newton Meter)
- **M_{max}** Maximum Bending Moment (Newton Meter)
- **M_p** Plastic Moment (Kilonewton Meter)
- **M'max** Maximum Moment (Newton Meter)
- **P** Point Load (Kilonewton)
- **q** Uniformly Distributed Load (Kilonewton per Meter)
- **t** Dam Thickness (Millimeter)
- **U** Ultimate Load (Kilonewton)
- **x** Distance of point where Moment is Maximum (Meter)
- **x''** Point of Maximum Moment (Meter)
- **Z** Section Modulus for Eccentric Load on Beam (Cubic Millimeter)
- **σ** Stress of Beam (Pascal)
- **Φ** Diameter of Circular Shaft (Millimeter)



Constants, Functions, Measurements used

- **Constant:** **pi**, 3.14159265358979323846264338327950288
Archimedes' constant
- **Function:** **sqrt**, sqrt(Number)
Square root function
- **Measurement:** **Length** in Millimeter (mm), Meter (m), Centimeter (cm)
Length Unit Conversion 
- **Measurement:** **Volume** in Cubic Millimeter (mm³)
Volume Unit Conversion 
- **Measurement:** **Area** in Square Millimeter (mm²)
Area Unit Conversion 
- **Measurement:** **Pressure** in Pascal (Pa), Megapascal (MPa), Newton per Square Meter (N/m²)
Pressure Unit Conversion 
- **Measurement:** **Force** in Kilonewton (kN)
Force Unit Conversion 
- **Measurement:** **Surface Tension** in Kilonewton per Meter (kN/m)
Surface Tension Unit Conversion 
- **Measurement:** **Moment of Inertia** in Kilogram Square Meter (kg·m²)
Moment of Inertia Unit Conversion 
- **Measurement:** **Moment of Force** in Newton Meter (N*m), Kilonewton Meter (kN*m)
Moment of Force Unit Conversion 



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