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# Simple Harmonic Motion Formulas

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# List of 22 Simple Harmonic Motion Formulas

## Simple Harmonic Motion

### Basics

#### 1) Frequency of Oscillation for SHM

$$\text{fx } f = \frac{1}{t_p}$$

Open Calculator 

$$\text{ex } 0.2\text{Hz} = \frac{1}{5\text{s}}$$

#### 2) Frequency of Particle Moving with Angular Simple Harmonic Motion

$$\text{fx } f = \frac{\sqrt{\frac{\alpha}{\theta}}}{2 \cdot \pi}$$

Open Calculator 

$$\text{ex } 0.200266\text{Hz} = \frac{\sqrt{\frac{190\text{rad/s}^2}{120\text{rad}}}}{2 \cdot \pi}$$



### 3) Periodic Time for SHM

$$fx \quad t_p = 2 \cdot \pi \cdot \sqrt{\frac{d_m}{g}}$$

[Open Calculator !\[\]\(cbe80b694ebd74fcfe136a095b608235\_img.jpg\)](#)

$$ex \quad 5.000031s = 2 \cdot \pi \cdot \sqrt{\frac{6206mm}{9.8m/s^2}}$$

### 4) Periodic Time of Particle Moving with Angular Simple Harmonic Motion

$$fx \quad t_p = 2 \cdot \pi \cdot \sqrt{\frac{\theta}{\alpha}}$$

[Open Calculator !\[\]\(3e2231b1ad3ca8da8658228c00dd08e0\_img.jpg\)](#)

$$ex \quad 4.993369s = 2 \cdot \pi \cdot \sqrt{\frac{120rad}{190rad/s^2}}$$

## Closely Coiled Helical Spring

### 5) Deflection of Spring when Mass m is Attached to it

$$fx \quad \delta = M \cdot \frac{g}{k}$$

[Open Calculator !\[\]\(b792654f2cef9719eabeb6c5be00811e\_img.jpg\)](#)

$$ex \quad 6164.753mm = 12.6kg \cdot \frac{9.8m/s^2}{20.03N/m}$$



## 6) Frequency of Mass Attached to Closely Coiled Helical Spring which is Hanged Vertically

$$fx \quad f = \frac{\sqrt{\frac{k}{M}}}{2 \cdot \pi}$$

[Open Calculator !\[\]\(e78f798d4ea5c530c9db49e7d26e6b95\_img.jpg\)](#)

$$ex \quad 0.200667Hz = \frac{\sqrt{\frac{20.03N/m}{12.6kg}}}{2 \cdot \pi}$$

## 7) Frequency of Mass Attached to Spring of given Mass

$$fx \quad f = \frac{\sqrt{\frac{k}{M + \frac{m}{3}}}}{2 \cdot \pi}$$

[Open Calculator !\[\]\(05be7c7a8995decd503647c99211f7c2\_img.jpg\)](#)

$$ex \quad 0.200402Hz = \frac{\sqrt{\frac{20.03N/m}{12.6kg + \frac{0.1kg}{3}}}}{2 \cdot \pi}$$

## 8) Periodic Time of Mass Attached to Closely Coiled Helical Spring which is Hanged Vertically

$$fx \quad t_p = 2 \cdot \pi \cdot \sqrt{\frac{M}{k}}$$

[Open Calculator !\[\]\(fe3aebe81acea8d45108cd2768939da7\_img.jpg\)](#)

$$ex \quad 4.983388s = 2 \cdot \pi \cdot \sqrt{\frac{12.6kg}{20.03N/m}}$$



## 9) Periodic Time of Mass Attached to Spring of given Mass

Open Calculator 

$$fx \quad t_p = 2 \cdot \pi \cdot \sqrt{\frac{M + \frac{m}{3}}{k}}$$

$$ex \quad 4.989975s = 2 \cdot \pi \cdot \sqrt{\frac{12.6kg + \frac{0.1kg}{3}}{20.03N/m}}$$

## 10) Restoring Force Due to Spring

Open Calculator 

$$fx \quad F = k \cdot x$$

$$ex \quad 2.50375N = 20.03N/m \cdot 125mm$$

## Compound Pendulum

### 11) Frequency of Compound Pendulum in SHM

Open Calculator 

$$fx \quad f = \frac{1}{t'_p}$$

$$ex \quad 0.2Hz = \frac{1}{5.00s}$$



## 12) Minimum Periodic Time of SHM for Compound Pendulum

[Open Calculator !\[\]\(eafc244b53721dd1ec133f0772f70fc7\_img.jpg\)](#)

$$fx \quad t_p = 2 \cdot \pi \cdot \sqrt{2 \cdot \frac{k_G}{g}}$$

$$ex \quad 5.000031s = 2 \cdot \pi \cdot \sqrt{2 \cdot \frac{3103mm}{9.8m/s^2}}$$

## 13) Periodic Time of SHM for Compound Pendulum given Radius of Gyration

[Open Calculator !\[\]\(10f8862fc183b400327470ea85afe9ae\_img.jpg\)](#)

$$fx \quad t'_p = 2 \cdot \pi \cdot \sqrt{\frac{k_G^2 + h^2}{g \cdot h}}$$

$$ex \quad 5.000032s = 2 \cdot \pi \cdot \sqrt{\frac{(3103mm)^2 + (3100mm)^2}{9.8m/s^2 \cdot 3100mm}}$$

## Simple Pendulum


### 14) Angular Acceleration of String

[Open Calculator !\[\]\(ab4e2b3fc7e7887b7a72f548aa6f5e60\_img.jpg\)](#)

$$fx \quad \alpha = g \cdot \frac{\theta}{L_s}$$

$$ex \quad 190.2913rad/s^2 = 9.8m/s^2 \cdot \frac{120rad}{6180mm}$$




15) Angular Frequency of Simple Pendulum 

$$fx \quad \omega = \sqrt{\frac{g}{L}}$$

[Open Calculator !\[\]\(9dfdaff1d86ba3c1f8353b4d1b61b8c5\_img.jpg\)](#)


$$ex \quad 2.745626\text{rad/s} = \sqrt{\frac{9.8\text{m/s}^2}{1300\text{mm}}}$$

16) Angular Frequency of Spring of given Stiffness Constant 

$$fx \quad \omega = \sqrt{\frac{K_s}{M}}$$

[Open Calculator !\[\]\(2b376d1a92330ab09dad2665d2f89bf5\_img.jpg\)](#)


$$ex \quad 2.01187\text{rad/s} = \sqrt{\frac{51\text{N/m}}{12.6\text{kg}}}$$

17) Periodic Time for One Beat of SHM 

$$fx \quad t_p = \pi \cdot \sqrt{\frac{L_s}{g}}$$

[Open Calculator !\[\]\(c444627dab9fee9a1550c053ffaaaae2\_img.jpg\)](#)

$$ex \quad 2.494773\text{s} = \pi \cdot \sqrt{\frac{6180\text{mm}}{9.8\text{m/s}^2}}$$

18) Restoring Torque for Simple Pendulum 

$$fx \quad \tau = M \cdot g \cdot \sin(\theta_d) \cdot L_s$$

[Open Calculator !\[\]\(06a315363e7801bba8c7489a6694af19\_img.jpg\)](#)

$$ex \quad 547.419\text{N}\cdot\text{m} = 12.6\text{kg} \cdot 9.8\text{m/s}^2 \cdot \sin(0.8\text{rad}) \cdot 6180\text{mm}$$



## Stiffness

### 19) Stiffness of Cantilever Beam

$$\text{fx } \kappa = \frac{3 \cdot E \cdot I}{L^3}$$

[Open Calculator !\[\]\(96cc62f861fdd6e50510c0224a756dff\_img.jpg\)](#)

$$\text{ex } 993.4001\text{N/m} = \frac{3 \cdot 15\text{N/m} \cdot 48.5\text{kg}\cdot\text{m}^2}{(1300\text{mm})^3}$$

### 20) Stiffness of Fixed-Fixed Beam with Load at Middle

$$\text{fx } K = \frac{192 \cdot E \cdot I}{L^3}$$

[Open Calculator !\[\]\(f95dab70c751fda7d824b8b03650f7aa\_img.jpg\)](#)

$$\text{ex } 17.3036\text{N/m} = \frac{192 \cdot 15\text{N/m} \cdot 0.0132\text{kg}\cdot\text{m}^2}{(1300\text{mm})^3}$$

### 21) Stiffness of Rod under Axial Load

$$\text{fx } K = \frac{E \cdot A_c}{L}$$

[Open Calculator !\[\]\(e9474ce1d70442456f8fe9c393ea149c\_img.jpg\)](#)

$$\text{ex } 17.30769\text{N/m} = \frac{15\text{N/m} \cdot 1.5\text{m}^2}{1300\text{mm}}$$





## 22) Stiffness of Tapered Rod under Axial Load

[Open Calculator !\[\]\(666e09182d4cd268646ea700ea60dcdf\_img.jpg\)](#)

$$\text{fx } K = \frac{\pi \cdot E \cdot d_1 \cdot d_2}{4 \cdot L}$$

$$\text{ex } 17.31441\text{N/m} = \frac{\pi \cdot 15\text{N/m} \cdot 466000.2\text{mm} \cdot 4.1\text{mm}}{4 \cdot 1300\text{mm}}$$



## Variables Used










- $A_c$  Rod Cross Sectional Area (Square Meter)
- $d_1$  End Diameter 1 (Millimeter)
- $d_2$  End Diameter 2 (Millimeter)
- $d_m$  Total Displacement (Millimeter)
- $E$  Young's Modulus (Newton per Meter)
- $f$  Frequency (Hertz)
- $F$  Force (Newton)
- $g$  Acceleration Due to Gravity (Meter per Square Second)
- $h$  Distance of PT of Suspension of Pendulum From CG (Millimeter)
- $I$  Moment of Inertia (Kilogram Square Meter)
- $k$  Stiffness of Spring (Newton per Meter)
- $K$  Stiffness Constant (Newton per Meter)
- $k_G$  Radius of Gyration (Millimeter)
- $K_s$  Spring Constant (Newton per Meter)
- $L$  Total Length (Millimeter)
- $L_s$  Length of String (Millimeter)
- $m$  Mass of Spring (Kilogram)
- $M$  Mass of Body (Kilogram)
- $t_p$  Time Period SHM (Second)
- $t'_p$  Periodic Time for Compound Pendulum (Second)
- $x$  Displacement of Load Below Equilibrium Position (Millimeter)
- $\alpha$  Angular Acceleration (Radian per Square Second)








- $\delta$  Deflection of Spring (*Millimeter*)
- $\theta$  Angular Displacement (*Radian*)
- $\theta_d$  Angle through which the String is Displaced (*Radian*)
- $I$  Moment of Inertia of Beam About Bending Axis (*Kilogram Square Meter*)
- $K$  Spring Constant of Cantilever Beam (*Newton per Meter*)
- $T$  Torque Exerted on Wheel (*Newton Meter*)
- $\omega$  Angular Frequency (*Radian per Second*)



## Constants, Functions, Measurements used









- **Constant:** **pi**, 3.14159265358979323846264338327950288  
*Archimedes' constant*
- **Function:** **sin**,  $\sin(\text{Angle})$   
*Sine is a trigonometric function that describes the ratio of the length of the opposite side of a right triangle to the length of the hypotenuse.*
- **Function:** **sqrt**,  $\text{sqrt}(\text{Number})$   
*A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.*
- **Measurement:** **Length** in Millimeter (mm)  
*Length Unit Conversion* 
- **Measurement:** **Weight** in Kilogram (kg)  
*Weight Unit Conversion* 
- **Measurement:** **Time** in Second (s)  
*Time Unit Conversion* 
- **Measurement:** **Area** in Square Meter ( $\text{m}^2$ )  
*Area Unit Conversion* 
- **Measurement:** **Acceleration** in Meter per Square Second ( $\text{m}/\text{s}^2$ )  
*Acceleration Unit Conversion* 
- **Measurement:** **Force** in Newton (N)  
*Force Unit Conversion* 
- **Measurement:** **Angle** in Radian (rad)  
*Angle Unit Conversion* 
- **Measurement:** **Frequency** in Hertz (Hz)  
*Frequency Unit Conversion* 
- **Measurement:** **Surface Tension** in Newton per Meter (N/m)  
*Surface Tension Unit Conversion* 



- **Measurement: Torque** in Newton Meter (N\*m)  
*Torque Unit Conversion* 
- **Measurement: Moment of Inertia** in Kilogram Square Meter (kg·m<sup>2</sup>)  
*Moment of Inertia Unit Conversion* 
- **Measurement: Angular Acceleration** in Radian per Square Second (rad/s<sup>2</sup>)  
*Angular Acceleration Unit Conversion* 
- **Measurement: Angular Frequency** in Radian per Second (rad/s)  
*Angular Frequency Unit Conversion* 
- **Measurement: Stiffness Constant** in Newton per Meter (N/m)  
*Stiffness Constant Unit Conversion* 



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