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Castigliano's Theorem for Deflection in Complex Structures Formulas

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List of 14 Castigliano's Theorem for Deflection in Complex Structures Formulas

Castigliano's Theorem for Deflection in Complex Structures

1) Cross-sectional Area of Rod given Strain Energy stored in Rod

$$fx \quad A = P^2 \cdot \frac{L}{2 \cdot U \cdot E}$$

Open Calculator 

$$ex \quad 552.6987\text{mm}^2 = (55000\text{N})^2 \cdot \frac{1432.449\text{mm}}{2 \cdot 37.13919\text{J} \cdot 105548.9\text{N}/\text{mm}^2}$$

2) Force Applied on Rod given Strain Energy Stored in Tension Rod

$$fx \quad P = \sqrt{U \cdot 2 \cdot A \cdot \frac{E}{L}}$$

Open Calculator 

$$ex \quad 55000\text{N} = \sqrt{37.13919\text{J} \cdot 2 \cdot 552.6987\text{mm}^2 \cdot \frac{105548.9\text{N}/\text{mm}^2}{1432.449\text{mm}}}$$

3) Length of Rod given Strain Energy Stored

$$fx \quad L = U \cdot 2 \cdot A \cdot \frac{E}{P^2}$$

Open Calculator 

$$ex \quad 1432.449\text{mm} = 37.13919\text{J} \cdot 2 \cdot 552.6987\text{mm}^2 \cdot \frac{105548.9\text{N}/\text{mm}^2}{(55000\text{N})^2}$$



4) Length of Shaft given Strain Energy Stored in Shaft Subjected to Bending Moment

$$fx \quad L = 2 \cdot U \cdot E \cdot \frac{I}{M_b^2}$$

[Open Calculator !\[\]\(cbe80b694ebd74fcfe136a095b608235_img.jpg\)](#)

$$ex \quad 1431.882\text{mm} = 2 \cdot 37.13919\text{J} \cdot 105548.9\text{N}/\text{mm}^2 \cdot \frac{552.5\text{mm}^4}{(55001\text{N} \cdot \text{mm})^2}$$

5) Length of Shaft when Strain Energy in Shaft Subjected to External Torque

$$fx \quad L = \frac{2 \cdot U \cdot J \cdot G}{\tau^2}$$

[Open Calculator !\[\]\(3e2231b1ad3ca8da8658228c00dd08e0_img.jpg\)](#)

$$ex \quad 1433.541\text{mm} = \frac{2 \cdot 37.13919\text{J} \cdot 553\text{mm}^4 \cdot 105591\text{N}/\text{mm}^2}{(55005\text{N} \cdot \text{mm})^2}$$

6) Modulus of Elasticity given Strain Energy Stored in Shaft Subjected to Bending Moment

$$fx \quad E = M_b^2 \cdot \frac{L}{2 \cdot U \cdot I}$$

[Open Calculator !\[\]\(0d5ec72f61334709c3fc9450209b754f_img.jpg\)](#)

$$ex \quad 105590.7\text{N}/\text{mm}^2 = (55001\text{N} \cdot \text{mm})^2 \cdot \frac{1432.449\text{mm}}{2 \cdot 37.13919\text{J} \cdot 552.5\text{mm}^4}$$



7) Modulus of Elasticity of Rod given Strain Energy Stored

$$fx \quad E = P^2 \cdot \frac{L}{2 \cdot A \cdot U}$$

[Open Calculator !\[\]\(e78f798d4ea5c530c9db49e7d26e6b95_img.jpg\)](#)

$$ex \quad 105548.9\text{N/mm}^2 = (55000\text{N})^2 \cdot \frac{1432.449\text{mm}}{2 \cdot 552.6987\text{mm}^2 \cdot 37.13919\text{J}}$$

8) Modulus of Rigidity of Rod given Strain Energy in Rod

$$fx \quad G = \tau^2 \cdot \frac{L}{2 \cdot J \cdot U}$$

[Open Calculator !\[\]\(05be7c7a8995decd503647c99211f7c2_img.jpg\)](#)

$$ex \quad 105510.6\text{N/mm}^2 = (55005\text{N*mm})^2 \cdot \frac{1432.449\text{mm}}{2 \cdot 553\text{mm}^4 \cdot 37.13919\text{J}}$$

9) Moment of Inertia of Shaft when Strain Energy Stored in Shaft Subjected to Bending Moment

$$fx \quad I = M_b^2 \cdot \frac{L}{2 \cdot E \cdot U}$$

[Open Calculator !\[\]\(fe3aebe81acea8d45108cd2768939da7_img.jpg\)](#)

$$ex \quad 552.7188\text{mm}^4 = (55001\text{N*mm})^2 \cdot \frac{1432.449\text{mm}}{2 \cdot 105548.9\text{N/mm}^2 \cdot 37.13919\text{J}}$$

10) Polar Moment of Inertia of Rod given Strain Energy in Rod

$$fx \quad J = \tau^2 \cdot \frac{L}{2 \cdot U \cdot G}$$

[Open Calculator !\[\]\(899d8b7697d64725bf017d3296cfcf1b_img.jpg\)](#)

$$ex \quad 552.5788\text{mm}^4 = (55005\text{N*mm})^2 \cdot \frac{1432.449\text{mm}}{2 \cdot 37.13919\text{J} \cdot 105591\text{N/mm}^2}$$




11) Strain Energy in Rod when it is Subjected to External Torque 

$$fx \quad U = \tau^2 \cdot \frac{L}{2 \cdot J \cdot G}$$

[Open Calculator !\[\]\(e2376d476d06eb31946dc01a69a4403a_img.jpg\)](#)

$$ex \quad 37.1109J = (55005N \cdot mm)^2 \cdot \frac{1432.449mm}{2 \cdot 553mm^4 \cdot 105591N/mm^2}$$

12) Strain Energy Stored in Rod Subjected to Bending Moment 

$$fx \quad U = M_b^2 \cdot \frac{L}{2 \cdot E \cdot I}$$

[Open Calculator !\[\]\(0b5e7e25e8775f7e7e80906ada4f0021_img.jpg\)](#)

$$ex \quad 37.1539J = (55001N \cdot mm)^2 \cdot \frac{1432.449mm}{2 \cdot 105548.9N/mm^2 \cdot 552.5mm^4}$$

13) Strain Energy Stored in Tension Rod 

$$fx \quad U = \frac{P^2 \cdot L}{2 \cdot A \cdot E}$$

[Open Calculator !\[\]\(bd3b31712ad9bab5a241210fa6925cdd_img.jpg\)](#)

$$ex \quad 37.13919J = \frac{(55000N)^2 \cdot 1432.449mm}{2 \cdot 552.6987mm^2 \cdot 105548.9N/mm^2}$$

14) Torque given Strain Energy in Rod Subjected to External Torque 

$$fx \quad \tau = \sqrt{2 \cdot U \cdot J \cdot \frac{G}{L}}$$

[Open Calculator !\[\]\(7bc43b319a082987e20f7bf78f4bab80_img.jpg\)](#)

$$ex \quad 55025.96N \cdot mm = \sqrt{2 \cdot 37.13919J \cdot 553mm^4 \cdot \frac{105591N/mm^2}{1432.449mm}}$$










Variables Used

- **A** Cross Sectional Area of Rod (*Square Millimeter*)
- **E** Modulus of Elasticity (*Newton per Square Millimeter*)
- **G** Modulus of Rigidity (*Newton per Square Millimeter*)
- **I** Area Moment of Inertia (*Millimeter⁴*)
- **J** Polar Moment of Inertia (*Millimeter⁴*)
- **L** Length of Rod or Shaft (*Millimeter*)
- **M_b** Bending Moment (*Newton Millimeter*)
- **P** Axial Force on Beam (*Newton*)
- **U** Strain Energy (*Joule*)
- **T** Torque (*Newton Millimeter*)








Constants, Functions, Measurements used

- **Function:** **sqrt**, $\text{sqrt}(\text{Number})$
A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.
- **Measurement:** **Length** in Millimeter (mm)
Length Unit Conversion 
- **Measurement:** **Area** in Square Millimeter (mm^2)
Area Unit Conversion 
- **Measurement:** **Energy** in Joule (J)
Energy Unit Conversion 
- **Measurement:** **Force** in Newton (N)
Force Unit Conversion 
- **Measurement:** **Torque** in Newton Millimeter ($\text{N}\cdot\text{mm}$)
Torque Unit Conversion 
- **Measurement:** **Second Moment of Area** in Millimeter⁴ (mm^4)
Second Moment of Area Unit Conversion 
- **Measurement:** **Stress** in Newton per Square Millimeter (N/mm^2)
Stress Unit Conversion 



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