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## CMOS Inverters Formulas

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## List of 16 CMOS Inverters Formulas

CMOS Inverters 1) Average Power Dissipation CMOS 

$$\text{fx } P_{\text{avg}} = C_{\text{load}} \cdot (V_{\text{DD}})^2 \cdot f$$

Open Calculator 


$$\text{ex } 0.404095\text{mW} = 0.93\text{fF} \cdot (3.3\text{V})^2 \cdot 39.9\text{GHz}$$

2) Average Propagation Delay CMOS 

$$\text{fx } \zeta_{\text{P}} = \frac{\zeta_{\text{PHL}} + \zeta_{\text{PLH}}}{2}$$

Open Calculator 

$$\text{ex } 0.004236\text{ns} = \frac{0.00229\text{ns} + 0.006182\text{ns}}{2}$$

3) Load Capacitance of Cascaded Inverter CMOS 

$$\text{fx } C_{\text{load}} = C_{\text{gd,p}} + C_{\text{gd,n}} + C_{\text{db,p}} + C_{\text{db,n}} + C_{\text{in}} + C_{\text{g}}$$

Open Calculator 

$$\text{ex } 0.93\text{fF} = 0.15\text{fF} + 0.1\text{fF} + 0.25\text{fF} + 0.2\text{fF} + 0.05\text{fF} + 0.18\text{fF}$$

4) Maximum Input Voltage CMOS 

$$\text{fx } V_{\text{IL}} = \frac{2 \cdot V_{\text{output}} + (V_{\text{T0,p}}) - V_{\text{DD}} + K_{\text{r}} \cdot V_{\text{T0,n}}}{1 + K_{\text{r}}}$$

Open Calculator 

$$\text{ex } 1.08\text{V} = \frac{2 \cdot 3.14\text{V} + (-0.7\text{V}) - 3.3\text{V} + 2.5 \cdot 0.6\text{V}}{1 + 2.5}$$

5) Maximum Input Voltage for Symmetric CMOS 

$$\text{fx } V_{\text{IL(sym)}} = \frac{3 \cdot V_{\text{DD}} + 2 \cdot V_{\text{T0,n}}}{8}$$

Open Calculator 

$$\text{ex } 1.3875\text{V} = \frac{3 \cdot 3.3\text{V} + 2 \cdot 0.6\text{V}}{8}$$

6) Minimum Input Voltage CMOS 

$$\text{fx } V_{\text{IH}} = \frac{V_{\text{DD}} + (V_{\text{T0,p}}) + K_{\text{r}} \cdot (2 \cdot V_{\text{out}} + V_{\text{T0,n}})}{1 + K_{\text{r}}}$$

Open Calculator 

$$\text{ex } 1.557143\text{V} = \frac{3.3\text{V} + (-0.7\text{V}) + 2.5 \cdot (2 \cdot 0.27\text{V} + 0.6\text{V})}{1 + 2.5}$$




7) Minimum Input Voltage for Symmetric CMOS 

$$\text{fx } V_{IH(\text{sym})} = \frac{5 \cdot V_{DD} - 2 \cdot V_{T0,n}}{8}$$

Open Calculator 

$$\text{ex } 1.9125\text{V} = \frac{5 \cdot 3.3\text{V} - 2 \cdot 0.6\text{V}}{8}$$

8) Noise Margin for High Signal CMOS 

$$\text{fx } N_{MH} = V_{OH} - V_{IH}$$

Open Calculator 


$$\text{ex } 1.8\text{V} = 3.35\text{V} - 1.55\text{V}$$

9) Oscillation Period Ring Oscillator CMOS 

$$\text{fx } T_{\text{osc}} = 2 \cdot n \cdot \zeta_P$$

Open Calculator 

$$\text{ex } 0.0252\text{ns} = 2 \cdot 3 \cdot 0.0042\text{ns}$$

10) Propagation Delay for High to Low Output Transition CMOS 

fx

Open Calculator 

$$\zeta_{\text{PHL}} = \left( \frac{C_{\text{load}}}{K_n \cdot (V_{DD} - V_{T,n})} \right) \cdot \left( \left( 2 \cdot \frac{V_{T,n}}{V_{DD} - V_{T,n}} \right) + \ln \left( \left( 4 \cdot \frac{V_{DD} - V_{T,n}}{V_{DD}} \right) - 1 \right) \right)$$

$$\text{ex } 0.002508\text{ns} = \left( \frac{0.93\text{fF}}{200\mu\text{A}/\text{V}^2 \cdot (3.3\text{V} - 0.8\text{V})} \right) \cdot \left( \left( 2 \cdot \frac{0.8\text{V}}{3.3\text{V} - 0.8\text{V}} \right) + \ln \left( \left( 4 \cdot \frac{3.3\text{V} - 0.8\text{V}}{3.3\text{V}} \right) - 1 \right) \right)$$

11) Propagation Delay for Low to High Output Transition CMOS 

fx

Open Calculator 

$$\zeta_{\text{PLH}} = \left( \frac{C_{\text{load}}}{K_p \cdot (V_{DD} - |V_{T,p}|)} \right) \cdot \left( \left( \frac{2 \cdot |V_{T,p}|}{V_{DD} - |V_{T,p}|} \right) + \ln \left( \left( 4 \cdot \frac{V_{DD} - |V_{T,p}|}{V_{DD}} \right) - 1 \right) \right)$$

$$\text{ex } 0.006765\text{ns} = \left( \frac{0.93\text{fF}}{80\mu\text{A}/\text{V}^2 \cdot (3.3\text{V} - |-0.9\text{V}|)} \right) \cdot \left( \left( \frac{2 \cdot |-0.9\text{V}|}{3.3\text{V} - |-0.9\text{V}|} \right) + \ln \left( \left( 4 \cdot \frac{3.3\text{V} - |-0.9\text{V}|}{3.3\text{V}} \right) - 1 \right) \right)$$


12) Resistive Load Maximum Input Voltage CMOS 

$$\text{fx } V_{IL(\text{RL})} = V_{T0} + \left( \frac{1}{K_n \cdot R_L} \right)$$

Open Calculator 


$$\text{ex } 1.4025\text{V} = 1.4\text{V} + \left( \frac{1}{200\mu\text{A}/\text{V}^2 \cdot 2\text{M}\Omega} \right)$$



13) Resistive Load Minimum Input Voltage CMOS [Open Calculator](#) 

$$\text{fx } V_{IH(RL)} = V_{T0} + \sqrt{\frac{8 \cdot V_{DD}}{3 \cdot K_n \cdot R_L}} - \left( \frac{1}{K_n \cdot R_L} \right)$$

$$\text{ex } 1.545824\text{V} = 1.4\text{V} + \sqrt{\frac{8 \cdot 3.3\text{V}}{3 \cdot 200\mu\text{A}/\text{V}^2 \cdot 2\text{M}\Omega}} - \left( \frac{1}{200\mu\text{A}/\text{V}^2 \cdot 2\text{M}\Omega} \right)$$

14) Resistive Load Minimum Output Voltage CMOS [Open Calculator](#) 

$$\text{fx } V_{OL(RL)} = V_{DD} - V_{T0} + \left( \frac{1}{K_n \cdot R_L} \right) - \sqrt{\left( V_{DD} - V_{T0} + \left( \frac{1}{K_n \cdot R_L} \right) \right)^2 - \left( 2 \cdot \frac{V_{DD}}{K_n \cdot R_L} \right)}$$

$$\text{ex } 0.004341\text{V} = 3.3\text{V} - 1.4\text{V} + \left( \frac{1}{200\mu\text{A}/\text{V}^2 \cdot 2\text{M}\Omega} \right) - \sqrt{\left( 3.3\text{V} - 1.4\text{V} + \left( \frac{1}{200\mu\text{A}/\text{V}^2 \cdot 2\text{M}\Omega} \right) \right)^2 - \left( 2 \cdot \frac{3.3\text{V}}{200\mu\text{A}/\text{V}^2 \cdot 2\text{M}\Omega} \right)}$$

15) Threshold Voltage CMOS [Open Calculator](#) 

$$\text{fx } V_{th} = \frac{V_{T0,n} + \sqrt{\frac{1}{K_r}} \cdot (V_{DD} + (V_{T0,p}))}{1 + \sqrt{\frac{1}{K_r}}}$$

$$\text{ex } 1.374852\text{V} = \frac{0.6\text{V} + \sqrt{\frac{1}{2.5}} \cdot (3.3\text{V} + (-0.7\text{V}))}{1 + \sqrt{\frac{1}{2.5}}}$$

16) Transconductance Ratio CMOS [Open Calculator](#) 

$$\text{fx } K_r = \frac{K_n}{K_p}$$

$$\text{ex } 2.5 = \frac{200\mu\text{A}/\text{V}^2}{80\mu\text{A}/\text{V}^2}$$



## Variables Used








- $C_{db,n}$  NMOS Drain Bulk Capacitance (Femtofarad)
- $C_{db,p}$  PMOS Drain Bulk Capacitance (Femtofarad)
- $C_g$  Inverter CMOS Gate Capacitance (Femtofarad)
- $C_{gd,n}$  NMOS Gate Drain Capacitance (Femtofarad)
- $C_{gd,p}$  PMOS Gate Drain Capacitance (Femtofarad)
- $C_{in}$  Inverter CMOS Internal Capacitance (Femtofarad)
- $C_{load}$  Inverter CMOS Load Capacitance (Femtofarad)
- $f$  Frequency (Gigahertz)
- $K_n$  Transconductance of NMOS (Microampere per Square Volt)
- $K_p$  Transconductance of PMOS (Microampere per Square Volt)
- $K_r$  Transconductance Ratio
- $n$  Number of Stages Ring Oscillator
- $N_{MH}$  Noise Margin for High Signal (Volt)
- $P_{avg}$  Average Power Dissipation (Milliwatt)
- $R_L$  Load Resistance (Megohm)
- $T_{osc}$  Oscillation Period (Nanosecond)
- $V_{DD}$  Supply Voltage (Volt)
- $V_{IH}$  Minimum Input Voltage (Volt)
- $V_{IH(RL)}$  Resistive Load Minimum Input Voltage (Volt)
- $V_{IH(sym)}$  Minimum Input Voltage Symmetric CMOS (Volt)
- $V_{IL}$  Maximum Input Voltage CMOS (Volt)
- $V_{IL(RL)}$  Resistive Load Maximum Input Voltage CMOS (Volt)
- $V_{IL(sym)}$  Maximum Input Voltage Symmetric CMOS (Volt)
- $V_{OH}$  Maximum Output Voltage (Volt)
- $V_{OL(RL)}$  Resistive Load Minimum Output Voltage (Volt)
- $V_{out}$  Output Voltage (Volt)
- $V_{output}$  Output Voltage for Max Input (Volt)
- $V_{T,n}$  Threshold Voltage of NMOS with Body Bias (Volt)
- $V_{T,p}$  Threshold Voltage of PMOS with Body Bias (Volt)
- $V_{T0}$  Zero Bias Threshold Voltage (Volt)
- $V_{T0,n}$  Threshold Voltage of NMOS Without Body Bias (Volt)
- $V_{T0,p}$  Threshold Voltage of PMOS Without Body Bias (Volt)



- $V_{th}$  Threshold Voltage (Volt)
- $\zeta_P$  Average Propagation Delay (Nanosecond)
- $\zeta_{PHL}$  Time for High to Low Transition of Output (Nanosecond)
- $\zeta_{PLH}$  Time for Low to High Transition of Output (Nanosecond)



## Constants, Functions, Measurements used

- **Function: abs**, abs(Number)  
*The absolute value of a number is its distance from zero on the number line. It's always a positive value, as it represents the magnitude of a number without considering its direction.*
- **Function: ln**, ln(Number)  
*The natural logarithm, also known as the logarithm to the base e, is the inverse function of the natural exponential function.*
- **Function: sqrt**, sqrt(Number)  
*A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.*
- **Measurement: Time** in Nanosecond (ns)  
*Time Unit Conversion* 
- **Measurement: Power** in Milliwatt (mW)  
*Power Unit Conversion* 
- **Measurement: Frequency** in Gigahertz (GHz)  
*Frequency Unit Conversion* 
- **Measurement: Capacitance** in Femtofarad (fF)  
*Capacitance Unit Conversion* 
- **Measurement: Electric Resistance** in Megohm (MΩ)  
*Electric Resistance Unit Conversion* 
- **Measurement: Electric Potential** in Volt (V)  
*Electric Potential Unit Conversion* 
- **Measurement: Transconductance Parameter** in Microampere per Square Volt ( $\mu\text{A}/\text{V}^2$ )  
*Transconductance Parameter Unit Conversion* 



## Check other formula lists

- [Array Datapath Subsystem Formulas](#) 
- [CMOS Circuit Characteristics Formulas](#) 
- [CMOS Delay Characteristics Formulas](#) 
- [CMOS Design Characteristics Formulas](#) 
- [CMOS Inverters Formulas](#) 
- [CMOS Power Metrics Formulas](#) 
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