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Governing Equations and Sound Wave Formulas

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List of 18 Governing Equations and Sound Wave Formulas

Governing Equations and Sound Wave

1) Critical Density

$$\text{fx } \rho_{\text{cr}} = \rho_o \cdot \left(\frac{2}{\gamma + 1} \right)^{\frac{1}{\gamma-1}}$$

Open Calculator 

$$\text{ex } 0.773405\text{kg/m}^3 = 1.22\text{kg/m}^3 \cdot \left(\frac{2}{1.4 + 1} \right)^{\frac{1}{1.4-1}}$$

2) Critical Pressure

$$\text{fx } P_{\text{cr}} = \left(\frac{2}{\gamma + 1} \right)^{\frac{\gamma}{\gamma-1}} \cdot P_o$$

Open Calculator 

$$\text{ex } 2.641409\text{at} = \left(\frac{2}{1.4 + 1} \right)^{\frac{1.4}{1.4-1}} \cdot 5\text{at}$$

3) Critical Temperature

$$\text{fx } T_{\text{cr}} = \frac{2 \cdot T_o}{\gamma + 1}$$

Open Calculator 

$$\text{ex } 250\text{K} = \frac{2 \cdot 300\text{K}}{1.4 + 1}$$



4) Flow Velocity Downstream of Sound Wave

[Open Calculator !\[\]\(4729e517bc6a7cd81c8025b9646574fb_img.jpg\)](#)

$$\text{fx } u_2 = \sqrt{2 \cdot \left(\frac{a_1^2 - a_2^2}{\gamma - 1} + \frac{u_1^2}{2} \right)}$$

$$\text{ex } 45.07716\text{m/s} = \sqrt{2 \cdot \left(\frac{(12\text{m/s})^2 - (31.90\text{m/s})^2}{1.4 - 1} + \frac{(80\text{m/s})^2}{2} \right)}$$

5) Flow Velocity Upstream of Sound Wave

[Open Calculator !\[\]\(e474458956c9a37fbf9586ddb60a7fa1_img.jpg\)](#)

$$\text{fx } u_1 = \sqrt{2 \cdot \left(\frac{a_2^2 - a_1^2}{\gamma - 1} + \frac{u_2^2}{2} \right)}$$

$$\text{ex } 79.95655\text{m/s} = \sqrt{2 \cdot \left(\frac{(31.90\text{m/s})^2 - (12\text{m/s})^2}{1.4 - 1} + \frac{(45\text{m/s})^2}{2} \right)}$$

6) Isentropic Change across Sound Wave

[Open Calculator !\[\]\(4fe57c3593bf1b21d272ae7ac8dfaf77_img.jpg\)](#)

$$\text{fx } dpd\rho = a^2$$

$$\text{ex } 117649\text{m}^2/\text{s}^2 = (343\text{m/s})^2$$



7) Isentropic Compressibility for given Density and Speed of Sound

$$fx \quad \tau_s = \frac{1}{\rho \cdot a^2}$$

[Open Calculator !\[\]\(e78f798d4ea5c530c9db49e7d26e6b95_img.jpg\)](#)

$$ex \quad 0.069387 \text{cm}^2/\text{N} = \frac{1}{1.225 \text{kg}/\text{m}^3 \cdot (343 \text{m}/\text{s})^2}$$

8) Mach Angle

$$fx \quad \mu = a \sin\left(\frac{1}{M}\right)$$

[Open Calculator !\[\]\(05be7c7a8995decd503647c99211f7c2_img.jpg\)](#)

$$ex \quad 30^\circ = a \sin\left(\frac{1}{2}\right)$$

9) Mach Number

$$fx \quad M = \frac{V_b}{a}$$

[Open Calculator !\[\]\(fe3aebe81acea8d45108cd2768939da7_img.jpg\)](#)

$$ex \quad 2.040816 = \frac{700 \text{m}/\text{s}}{343 \text{m}/\text{s}}$$


10) Mayer's Formula

$$fx \quad R = C_p - C_v$$

[Open Calculator !\[\]\(899d8b7697d64725bf017d3296cfcf1b_img.jpg\)](#)

$$ex \quad 273 \text{J}/(\text{kg} \cdot \text{K}) = 1005 \text{J}/(\text{kg} \cdot \text{K}) - 732 \text{J}/(\text{kg} \cdot \text{K})$$




11) Ratio of Stagnation and Static Density 

$$\text{fx } \rho_r = \left(1 + \left(\frac{\gamma - 1}{2} \right) \cdot M^2 \right)^{\frac{1}{\gamma-1}}$$

Open Calculator 


$$\text{ex } 4.346916 = \left(1 + \left(\frac{1.4 - 1}{2} \right) \cdot (2)^2 \right)^{\frac{1}{1.4-1}}$$

12) Ratio of Stagnation and Static Pressure 

$$\text{fx } P_r = \left(1 + \left(\frac{\gamma - 1}{2} \right) \cdot M^2 \right)^{\frac{\gamma}{\gamma-1}}$$

Open Calculator 

$$\text{ex } 7.824449 = \left(1 + \left(\frac{1.4 - 1}{2} \right) \cdot (2)^2 \right)^{\frac{1.4}{1.4-1}}$$

13) Ratio of Stagnation and Static Temperature 

$$\text{fx } T_r = 1 + \left(\frac{\gamma - 1}{2} \right) \cdot M^2$$

Open Calculator 

$$\text{ex } 1.8 = 1 + \left(\frac{1.4 - 1}{2} \right) \cdot (2)^2$$



14) Speed of Sound 

$$fx \quad a = \sqrt{\gamma \cdot [\text{R-Dry-Air}] \cdot T_s}$$

Open Calculator 

$$ex \quad 344.9012\text{m/s} = \sqrt{1.4 \cdot [\text{R-Dry-Air}] \cdot 296\text{K}}$$

15) Speed of Sound Downstream of Sound Wave 

$$fx \quad a_2 = \sqrt{(\gamma - 1) \cdot \left(\frac{u_1^2 - u_2^2}{2} + \frac{a_1^2}{\gamma - 1} \right)}$$

Open Calculator 

ex

$$31.92178\text{m/s} = \sqrt{(1.4 - 1) \cdot \left(\frac{(80\text{m/s})^2 - (45\text{m/s})^2}{2} + \frac{(12\text{m/s})^2}{1.4 - 1} \right)}$$

16) Speed of Sound given Isentropic Change 

$$fx \quad a = \sqrt{dpd\rho}$$

Open Calculator 

$$ex \quad 343\text{m/s} = \sqrt{117649\text{m}^2/\text{s}^2}$$



17) Speed of Sound Upstream of Sound Wave Open Calculator 

$$\text{fx } a_1 = \sqrt{(\gamma - 1) \cdot \left(\frac{u_2^2 - u_1^2}{2} + \frac{a_2^2}{\gamma - 1} \right)}$$

ex

$$11.94194\text{m/s} = \sqrt{(1.4 - 1) \cdot \left(\frac{(45\text{m/s})^2 - (80\text{m/s})^2}{2} + \frac{(31.90\text{m/s})^2}{1.4 - 1} \right)}$$

18) Stagnation Temperature Open Calculator 

$$\text{fx } T_0 = T_s + \frac{U_{\text{fluid}}^2}{2 \cdot C_p}$$

$$\text{ex } 297.0119\text{K} = 296\text{K} + \frac{(45.1\text{m/s})^2}{2 \cdot 1005\text{J}/(\text{kg} \cdot \text{K})}$$



Variables Used







- **a** Speed of Sound (Meter per Second)
- **a₁** Sound Speed Upstream (Meter per Second)
- **a₂** Sound Speed Downstream (Meter per Second)
- **C_p** Specific Heat Capacity at Constant Pressure (Joule per Kilogram per K)
- **C_v** Specific Heat Capacity at Constant Volume (Joule per Kilogram per K)
- **dpdp** Isentropic Change (Square Meter per Square Second)
- **M** Mach Number
- **P₀** Stagnation Pressure (Atmosphere Technical)
- **p_{cr}** Critical Pressure (Atmosphere Technical)
- **P_r** Stagnation to Static Pressure
- **R** Specific Gas Constant (Joule per Kilogram per K)
- **T₀** Stagnation Temperature (Kelvin)
- **T_{cr}** Critical Temperature (Kelvin)
- **T_r** Stagnation to Static Temperature
- **T_s** Static Temperature (Kelvin)
- **u₁** Flow Velocity Upstream of Sound (Meter per Second)
- **u₂** Flow Velocity Downstream of Sound (Meter per Second)
- **U_{fluid}** Velocity of Fluid Flow (Meter per Second)
- **V_b** Speed of Object (Meter per Second)
- **γ** Specific Heat Ratio
- **μ** Mach Angle (Degree)
- **ρ** Density (Kilogram per Cubic Meter)



- ρ_{cr} Critical Density (Kilogram per Cubic Meter)
- ρ_o Stagnation Density (Kilogram per Cubic Meter)
- ρ_r Stagnation to Static Density
- τ_s Isentropic Compressibility (Square Centimeter per Newton)



Constants, Functions, Measurements used

- **Constant:** [R-Dry-Air], 287.058
Specific Gas Constant for Dry Air
- **Function:** **asin**, asin(Number)
The inverse sine function, is a trigonometric function that takes a ratio of two sides of a right triangle and outputs the angle opposite the side with the given ratio.
- **Function:** **sin**, sin(Angle)
Sine is a trigonometric function that describes the ratio of the length of the opposite side of a right triangle to the length of the hypotenuse.
- **Function:** **sqrt**, sqrt(Number)
A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.
- **Measurement:** **Temperature** in Kelvin (K)
Temperature Unit Conversion 
- **Measurement:** **Pressure** in Atmosphere Technical (at)
Pressure Unit Conversion 
- **Measurement:** **Speed** in Meter per Second (m/s)
Speed Unit Conversion 
- **Measurement:** **Angle** in Degree (°)
Angle Unit Conversion 
- **Measurement:** **Specific Heat Capacity** in Joule per Kilogram per K (J/(kg*K))
Specific Heat Capacity Unit Conversion 
- **Measurement:** **Density** in Kilogram per Cubic Meter (kg/m³)
Density Unit Conversion 
- **Measurement:** **Specific Energy** in Square Meter per Square Second (m²/s²)



Specific Energy Unit Conversion 

- **Measurement: Compressibility** in Square Centimeter per Newton (cm^2/N)

Compressibility Unit Conversion 



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- [Governing Equations and Sound Wave Formulas](#) 
- [Oblique Shock and Expansion Waves Formulas](#) 
- [Normal Shock Wave Formulas](#) 

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